| Estd. 1894      | P.R.Government College<br>(Autonomous):<br>KAKINADA |   |   | <b>Seme</b><br>(ISem) |   |
|-----------------|---|---|---|-----------------------|---|
| Course Code     | TITLEOFTHECOURSE                                    |   |   |                       |   |
| MAT-101/1201    | Differential Equations                              |   |   |                       |   |
| Teaching        | HoursAllocated:60( <b>Theory</b> )                  | L | T | P                     | С |
| Pre-requisites: | Basic Mathematics Knowledge                         | 4 | 0 | 1                     | 4 |

#### Course Objectives:

To provide students with an introduction to the theory of ordinary differential equations through applications, methods of solution, and numerical approximations.

#### Course Outcomes:

| On Co | ompletion of the course, the students will be able to-  |
|-------|---|
| C01   | Solve linear differential equations   |
| CO2   | Convert non - exact homogeneous equations to exact differential equations by using integrating factors.         |
| CO3   | Know the methods of finding solutions of differential equations of the first order but not of the first degree. |
| CO4   | Understand the concept and apply appropriate methods for solving differential equations.                        |

#### Course with focus on employability/entrepreneurship /Skill Development modules

| Skill<br>Development | Employability |  | Entrepreneurship |  |
|----------------------|---------------|--|------------------|--|
|----------------------|---------------|--|------------------|--|

#### **COURSE SYLLABUS:**

UNIT – I: Differential Equations of first order and first degree (12 Hours)

Linear Differential Equations; Differential equations reducible to linear form; Exact differential equations; Integrating factors.

UNIT – II: Orthogonal Trajectory and Differential Equations of first order but not of the first degree (12 Hours)

Orthogonal Trajectories, Equations solvable for p; Equations solvable for y; Equations solvable for x; Equations of the first degree in x and y – Clairaut's Equation.

#### UNIT – III: Higher order linear differential equations-I

**(12 Hours)** 

Solution of homogeneous linear differential equations of order n with constant coefficients; Solution of the non-homogeneous linear differential equations with constant coefficients by means of polynomial operators. General Solution of f(D)y=0. General Solution of f(D)y=0 when Q is a function of f(D)y=0 when Q is a function of f(D)y=0.

**P.I.** of f(D)y = Q when  $Q = be^{ax}$ 

P.I. of f(D)y = Q when Q is  $b \sin ax$  or  $b \cos ax$ .

#### UNIT - IV: Higher order linear differential equations-II

**(12 Hours)** 

Solution of the non-homogeneous linear differential equations with constant coefficients.

P.I. of f(D)y = Q when  $Q = b x^k$ 

P.I. of f(D)y = Q when  $Q = e^{ax} V$ , where V is a function of x.

P.I. of f(D)y = Q when Q = x V, where V is a function of x.

UNIT -V: Higher order linear differential equations-III

**(12 Hours)** 

Method of variation of parameters; The Cauchy-Euler Equation, Legendre's linear equations.

#### Co-Curricular Activities:

**(15 Hours)** 

Seminar/ Quiz/ Assignments/ Applications of Differential Equations to Real life Problem / Problem Solving.

#### **Prescribed Text Book:**

Differential Equations and Their Applications by Zafar Ahsan, published by Prentice-Hall of India Pvt. Ltd, New Delhi-Second edition.

#### Reference Books:

- 1. A text book of Mathematics for B.A/B.Sc, Vol 1, by N. Krishna Murthy & others, published by S. Chand & Company, New Delhi.
- 2. Ordinary and Partial Differential Equations by Dr. M.D,Raisinghania, published by S. Chand & Company, New Delhi.
- 3. Differential Equations with applications and programs S. Balachandra Rao & HR Anuradha- Universities Press.
- 4. Differential Equations -Srinivas Vangala & Madhu Rajesh, published by Spectrum University Press.

#### Additional Inputs :

**Total Differential Equations** 

## CO-POMapping:

(1:Slight[Low]; 2:Moderate[Medium]; 3:Substantial[High], '-':NoCorrelation)

|   |     | P01 | P02 | P03 | P04 | P05 | P06 | P07 | P08 | P09 | P010 | PSO1 | PSO2 | PSO3 |
|---|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|------|------|------|------|
|   | CO1 | 3   | 3   | 2   | 3   | 3   | 3   | 1   | 2   | 2   | 3    | 2    | 3    | 2    |
|   | CO2 | 3   | 2   | 3   | 3   | 2   | 3   | 3   | 1   | 3   | 3    | 3    | 2    | 1    |
| Ī | CO3 | 2   | 3   | 2   | 3   | 2   | 3   | 2   | 2   | 2   | 3    | 2    | 2    | 3    |
|   | CO4 | 3   | 2   | 3   | 2   | 2   | 2   | 3   | 3   | 1   | 1    | 3    | 1    | 2    |

# BLUE PRINT FOR QUESTION PAPER PATTERN COURSE-I, DIFFERENTIAL EQUATIONS

| Unit | ТОРІС   | S.A.Q | E.Q | Marks allotted<br>to the Unit |
|------|---|-------|-----|-------------------------------|
| I    | Differential Equations of first order and first degree            | 2     | 2   | 20                            |
| II   | Differential Equations of first order but not of the first degree | 2     | 2   | 20                            |
| III  | Higher order linear differential equations-I                      | 2     | 2   | 20                            |
| IV   | Higher order linear differential equations-II                     | 1     | 2   | 16                            |
| V    | Higher order linear differential equations-III                    | 1     | 2   | 16                            |
|      | Total   | 8     | 10  | 92                            |

**S.A.Q.** = Short answer questions (4 marks)

**E.Q** = Essay questions (6 marks)

Short answer questions : 5X4= 20M

Essay questions : 5X6=30M

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Total Marks = 50M

#### P.R. GOVT. COLLEGE (AUTONOMOUS), KAKINADA

I year B.Sc., Degree Examinations - I Semester

#### **Mathematics Course-I: Differential Equations**

(w.e.f. 2022-23 Admitted Batch) Model Paper (w.e.f. 2022-2023)

••••••••••••••••••••••••••••••••••••

Time: 2Hrs 30 min Max. Marks: 50M

#### PART - I

Answer any FIVE questions. Each question carries FORE marks.

5 X 4=20M

1. Solve 
$$(y - e^{\sin^{-1}x})\frac{dx}{dy} + \sqrt{1 - x^2} = 0$$

2. Solve 
$$(x^2 + y^2 + 2x)dx + 2y dy = 0$$

- 3. Solve  $y + px = p^2x^4$
- 4. Find the Orthogonal trajectories of family of curves  $r = a(1 + \cos\theta)$ .
- 5. Solve  $(D^2 3D + 2) = \cos hx$
- 6. Solve  $(D^3 + 2D^2 + D)y = e^{2x}$
- 7. Solve $(D^2 4D + 4)y = x^3$
- 8. Solve  $(x^2D^2 xD + 1)y = 2 \log x$

#### PART - II

Answer the following questions. Each question carries SIX marks.

5 X 6=30M

9. Solve 
$$(xy^3 + y)dx + 2(x^2y^2 + x + y^4)dy = 0$$
 (OR)

10. Solve 
$$\frac{dy}{dx}(x^2y^3 + xy) = 1$$

11. Solve 
$$p^2 + 2py \cot x = y^2$$

(OR)

- 12. Find the orthogonal trajectories of the family of curves  $x^{\frac{2}{3}} + y^{\frac{2}{3}} = a^{\frac{2}{3}}$ , where a is the parameter.
- 13. Solve  $(D^2 + a^2)y = tanax$ .

(OR)

14. Solve 
$$(D^2 - 4D + 3)y = \sin 3x \cos 2x$$
.

15. Solve 
$$(D^2 - 2D + 4)y = 8(x^2 + e^{2x} + \sin 2x)$$

(OR)

16. Solve 
$$(D^2 - 4D + 4)y = 8x^2e^{2x}sin2x$$

17. Solve  $(D^2 - 2D)y = e^x \sin x$  by the method of variation of parameters.

(OR)

18. Solve [ 
$$(1 + x)^2 D^2 + (1 + x)D + 1$$
 ]  $y = 4 \cos \log (1 + x)$ .

| Estd. 1884           | P.R.Government College<br>(Autonomous)<br>KAKINADA | Program & Semester  IB.Sc. (ISem)  w.e.f.2022-23 admitted  Batch |   |   |   |  |
|----------------------|--|--|---|---|---|--|
| Course Code MAT-101P | TITLE OF THE COURSE  Differential Equations        |  | 2 |   |   |  |
| Teaching             | Hours Allocated:30(Practical's)                    | L  | T | P | С |  |
| Pre-requisites:      | Basic Mathematics Knowledge                        | -  | - | 2 | 1 |  |

#### UNIT – I: Differential Equations of first order and first degree

- Linear Differential Equations
- > Differential equations reducible to linear form
- > Exact differential equations
- > Integrating factors

# UNIT – II: Orthogonal Trajectory and Differential Equations of first order but not of the first degree

- Orthogonal Trajectories
- $\triangleright$  Equations solvable for p
- > Equations solvable for y
- $\triangleright$  Equations solvable for x
- $\triangleright$  Equations of the first degree in x and y Clairaut's Equation

#### UNIT – III: Higher order linear differential equations-I

- > Solution of homogeneous linear differential equations of order n with constant coefficients
- >. Solution of the non-homogeneous linear differential equations with constant coefficients by means of polynomial operators.
- $\triangleright$  General Solution of f(D)y=0
- Figure General Solution of f(D)y=Q when Q is a function of x,  $\frac{1}{f(D)}$  is expressed as partial fractions.
- ightharpoonup P.I. of f(D)y = Q when  $Q = be^{ax}$
- $\triangleright$  P.I. of f(D)y = Q when Q is  $b \sin ax$  or  $b \cos ax$ .

#### UNIT - IV: Higher order linear differential equations-

- $\triangleright$  P.I. of f(D)y = Q when  $Q = b x^k$
- $\triangleright$  P.I. of f(D)y = Q when  $Q = e^{ax} V$ , where V is a function of x.
- $\triangleright$  P.I. of f(D)y = Q when Q = x V, where V is a function of x.

### UNIT -V: Higher order linear differential equations-III

- > Method of variation of parameters
- > The Cauchy-Euler Equation
- > Legendre's linear equations.

# BLUE PRINT FOR PRACTICAL PAPER PATTERN COURSE-I, DIFFERENTIAL EQUATIONS

| Unit | TOPIC   | E.Q | Marks allotted to the Unit |
|------|---|-----|----------------------------|
| I    | Differential Equations of first order and first degree            | 2   | 12                         |
| II   | Differential Equations of first order but not of the first degree | 2   | 12                         |
| III  | Higher order linear differential equations-I                      | 1   | 06                         |
| IV   | Higher order linear differential equations-II                     | 2   | 12                         |
| V    | Higher order linear differential equations-III                    | 1   | 06                         |
|      | Total   | 08  | 48                         |

## Semester – I end Practical Examinations Scheme of Valuation for Practical's

Time: 2 Hours Max. Marks: 50

Record - 10 Marks
 Viva voce - 10 Marks
 Test - 30 Marks

Answer any 5questions. At least 2 questions from each section. Each question carries 6 marks.

#### P.R. GOVT. COLLEGE (AUTONOMOUS), KAKINADA

### I year B.Sc., Degree Examinations - I Semester Mathematics Course-I: Differential Equations (w.e.f. 2022-23 Admitted Batch) Practical Model Paper (w.e.f. 2022-2023)

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Time: 2Hrs Max. Marks: 50M

# Answer any 5questions. At least 2 questions from each section. SECTION - A

 $5 \times 6 = 30 \text{ Marks}$ 

- 1. Solve  $\frac{dy}{dx} (x^2 y^3 + xy) = 1$
- 2. Solve  $x^2y dx (x^3 + y^3)dy = 0$ .
- 3. Show that the family of confocal conics  $\frac{x^2}{a^2 + \lambda} + \frac{y^2}{b^2 + \lambda} = 1$  is self-orthogonal, where  $\lambda$

is the Parameter.

4. Solve  $2px = 2 \tan y + p^3 \cos^2 y$ 

#### **SECTION - B**

- 5. Solve  $(D^2 4D + 3)y = \sin 3x \cos 2x$ .
- 6. Solve  $(D^2 4D + 4)y = 8x^2e^{2x}sin2x$
- 7. Solve (  $D^4 + 2D^2 + 1$  )  $y = x^2 \cos x$
- 8. Solve [  $(1 + x)^2 D^2 + (1 + x)D + 1$  ]  $y = 4 \cos \log (1 + x)$ .
  - ➤ Record 10 Marks
  - ➤ Viva voce 10 Marks